Summer Work Packet for MPH Math Classes

Students going into Geometry Sept. 2019

This packet is designed to help students stay current with their math skills.

Each math class expects a certain level of number sense, algebra sense and graph sense in order to be successful in the course.

These problems need to be completed in the space provided, or on a separate sheet of paper, by the first day of class. Be sure to show all work.

Students can expect this packet to be graded, and/or to have a test on this material during the first marking period. If you have any questions, please email Mrs. Reeve at sreeve@mphschool.org

Supply List for Geometry

TI-84 or TI-84⁺ calculator

Pencils/pens

Colored pencils

3 ring binder (Can be shared with another class)

3 ring binder pencil pouch

Protractor

Quality compass -- Compasses with a wheel between the arms are strongly preferred, as they prevent slippage, which is important for successful constructions.

Show all work! Do NOT round any answers. Write the answers as a fraction if the decimal is repeating or the calculator does not show the whole decimal.

Evaluate each expression. Find the answer and show your work. Remember Order of Operations: Grouping, Exponents, Multiplication and Division, then Addition and Subtraction, all from left to right.

1.
$$40 - \frac{20 - 3(5)}{5} + 3(2 - 6)^2 =$$

2. If
$$a = 6$$
, $b = -2$, and $c = 8$; $\frac{2(a-c)}{b+4} =$

Translate into algebra.

3. Five times a certain number is half a different number.

Simplify. Show all your work. Remember, you need an LCD to add or subtract fractions.

4.
$$\frac{7}{9} - \frac{4}{5} =$$

5.
$$\frac{6}{5} + 2\frac{5}{8} =$$

6.
$$\frac{8}{9} \div \frac{2}{3}$$

$$7.\left(\frac{-5}{7}\right)\left(\frac{3}{10}\right) =$$

Simplify each expression.

8.
$$7b - 6c - 3c =$$

9.
$$(n^6)(n^4) =$$

10.
$$\frac{c^{50}}{c^{40}} =$$

11.
$$\frac{12a^6}{4a}$$

Solve each equation. Show all your work and CHECK!

12.
$$6x = -3x + 7$$

13.
$$4h = -2(3h + 5)$$

Check:

Check:

14.
$$18 = -3y$$

15.
$$\frac{x}{-5} = 8$$

Check:

Check:

16.
$$\frac{2x-8}{2} = 5$$

17.
$$6x - 9 = x + 11$$

Check:

Check:

18.
$$-5(3-x) = 3x + 1$$

Check:

Solve each inequality and graph the solution on a number line. Show all your work. Remember, if you multiply or divide by a negative number you must switch the direction of the inequality sign.

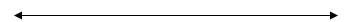
19.
$$x - (-4) > 9$$



20.
$$\frac{x}{-2} < 3$$



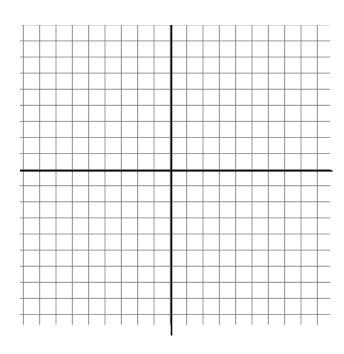
21.
$$9n + 3 < 3n - 15$$



22.
$$3n + 5 \ge -4$$

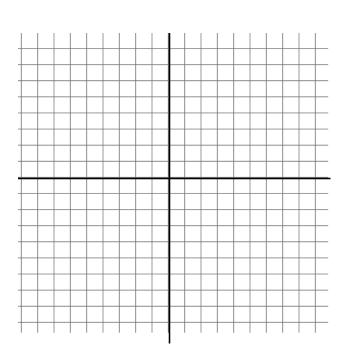
Graph the equation. Use a table or the slope-intercept method, y = mx + b.

23.
$$y = -2x + 3$$



Graph the inequality. Don't forget to shade and to show your check.

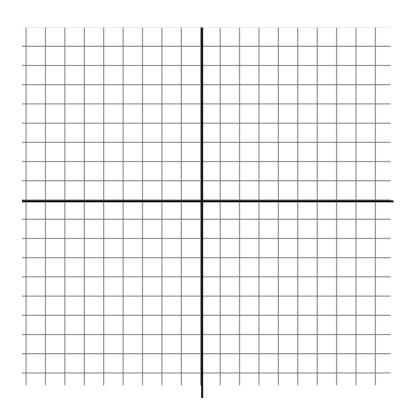
24.
$$y \le 2x - 3$$



Find the slope of the line containing the points.

Find the **x-intercept and y-intercept**. **Graph** the points. Find the **slope** of the line through the points. Write the equation in **slope-intercept** (y = mx + b) form.

26.
$$6x - 4y = 12$$



Simplify the following expressions.

Example:
$$3(m^2 + n) - 2(3m^2 - 4n) = 3m^2 + 3n - 6m^2 + 8n = -3m^2 + 11n$$

27.
$$(3x^2 + 4x - 5xy) + (-7x^2 + 6x - 5xy)$$

28.
$$(5y^3 - 3y + 4) + (2y^2 + 6y - 4y^3) - (9y^2 - 6 + 2y^3)$$

29.
$$(-2x^7)(3x^4)$$

$$30. \quad \frac{12x^3y^4z^5}{2x^5y^4z^2}$$

Use the distributive property to expand the product. Follow the example.

EXAMPLE:
$$(x + 4)(2x - 11) = 2x^2 - 11x + 8x - 44 = 2x^2 - 3x - 44$$

31.
$$(x-7)(x+5)$$

32.
$$(y-8)(y+8)$$

33.
$$(2x+5)(3x-4)$$

Factor each into the product of two binomials. Follow the example.

EXAMPLE:
$$x^2 + 6x - 7 = (x - 1)(x + 7)$$

34.
$$x^2 - 10x + 24$$

35.
$$x^2 - 81$$

36.
$$x^2 - 8x - 20$$

37.
$$x^2 + 13x + 36$$

Factor each and solve for x. Follow the example.

EXAMPLE:
$$x^2 + 5x - 6 = 0$$

 $(x + 6)(x - 1) = 0$
 $(x + 6) = 0$ OR $(x - 1) = 0$
 $x = -6$ OR $x = 1$

Factored and equal to 0
<u>Either</u> factor may equal 0

38.
$$x^2 + 6x + 8 = 0$$

$$39. \quad x^2 - 3x - 4 = 0$$

40.
$$x^2 - 15x + 50 = 0$$

41.
$$x^2 + x - 12 = 0$$

Solve by the graphing, substitution or elimination method.

EXAMPLE Substitution: y = 3x - 4 and 8x - 2y = 10 8x - 2(3x - 4) = 10 Substitute the value for y 8x - 6x + 8 = 10 2x + 8 = 10 2x = 2 x = 1 Finish solving: y = 3(1) - 4 so y = -1. Then CHECK! 8(1) - 2(-1) = 108 + 2 = 10 yes

EXAMPLE Elimination:
$$4x + 6y = 12$$

$$4x - 8y = 5$$

$$14y = 7$$

$$y = \frac{1}{2}$$
Finish solving for x: $4x + 6(.5) = 12$, so $x = 9/4$.
Then CHECK! $4(9/4) - 8(\frac{1}{2}) = 5$

$$9 - 4 = 5$$
 yes

$$42. \qquad 2y + x = 5$$
$$y = 3x - 1$$

Check:

$$43. \qquad \begin{aligned} x &= 3 + y \\ x - 7y &= 45 \end{aligned}$$

Check:

44.
$$5x + 2y = 13$$
$$5x + 4y = 11$$

Check:

RULES FOR SIMPLIFYING RADICALS (square roots)

$$a\sqrt{b} \times c\sqrt{d} = ac\sqrt{bd}$$

$$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{a/b}$$

$$a\sqrt{b} \times c\sqrt{d} = ac\sqrt{bd}$$
 $\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{a/b}$ $\sqrt{a} \times \sqrt{a} = \sqrt{a^2} = |a|$

$$a\sqrt{b} + c\sqrt{b} = (a+c)\sqrt{b}$$

Remember, proper form for radicals means:

- a. No perfect square factor under the radical. For example, $\sqrt{45} = \sqrt{9} \times \sqrt{5} = 3\sqrt{5}$
- b. No fractions/decimals may be left under the radical. For example, $\sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{\sqrt{4}} = \frac{\sqrt{3}}{2}$.
- c. No radical may be left in the denominator of a fraction. For example,

$$\sqrt{\frac{3}{7}} = \frac{\sqrt{3}}{\sqrt{7}} = \frac{\sqrt{3}}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}} = \frac{\sqrt{21}}{7}. \text{ Another example, } \frac{15\sqrt{75}}{20\sqrt{21}} = \frac{3\sqrt{25}\sqrt{3}}{4\sqrt{7}\sqrt{3}} = \frac{3\times5}{4\sqrt{7}} = \frac{3\times5\times\sqrt{7}}{4\sqrt{7}\sqrt{7}} = \frac{15\sqrt{7}}{28}.$$

Simplify each. Leave in best radical form. NO DECIMAL EQUIVALENTS.

45.
$$\sqrt{32}$$

46.
$$\frac{\sqrt{64}}{\sqrt{16}}$$

47.
$$\sqrt{20} - \sqrt{80}$$

48.
$$4\sqrt{5} \times 3\sqrt{10}$$

49.
$$\frac{\sqrt{18}}{\sqrt{24}}$$

50.
$$\frac{8\sqrt{3}}{\sqrt{2}}$$

Write an equation and solve. Example: What is 24% of 70? $x = .24 \times 70$, $x = 16.8$	
51.	What is 30% of 210?
52.	18 is what percent of 45?
53.	16.8 is 28% of what number?
	Enjoy your summer. See you in the Fall!