Summer Work Packet for MPH Math Classes

Students going into Geometry S Sept. 2021

This packet is designed to help students stay current with their math skills.

Each math class expects a certain level of number sense, algebra sense, and graph sense in order to be successful in the course.

These problems need to be completed in the space provided, or on a separate sheet of paper, by the first day of class. Be sure to show all work.

If you have any questions, please email Mrs. Meehan at dmeehan@mphschool.org.

Supply List for Geometry

- TI-84⁺ calculator
- Pencils/pens
- Colored pencils
- 3 ring binder (can be shared with another class), paper, graph paper
- Protractor
- Quality compass -- Compasses with a wheel between the arms are strongly preferred, as they prevent slippage, which is important for successful constructions.

Show all work! Do NOT round any answers. Write the answers as a fraction if the decimal is repeating, or the calculator does not show the whole decimal.

Evaluate each expression. Find the answer and show your work. Remember Order of Operations: Grouping, Exponents, Multiplication and Division, then Addition and Subtraction, all from left to right.

1.
$$40 - \frac{20 - 3(5)}{5} + 3(2 - 6)^2 =$$

2. If
$$a = 6$$
, $b = -2$, and $c = 8$, then $\frac{2(a-c)}{b+4} = \underline{\hspace{1cm}}$.

Translate into algebra.

3. Five times a certain number is half a different number.

Simplify. Show all your work. Remember, you need an LCD to add or subtract fractions.

4.
$$\frac{7}{9} - \frac{4}{5} =$$

5.
$$\frac{6}{5} + 2\frac{5}{8} =$$

6.
$$\frac{8}{9} \div \frac{2}{3}$$

$$7.\left(\frac{-5}{7}\right)\left(\frac{3}{10}\right) =$$

Simplify each expression.

8.
$$7b - 6c - 3c =$$

9.
$$(n^6)(n^4) =$$

10.
$$\frac{c^{50}}{c^{40}} =$$

11.
$$\frac{12a}{4a}$$

Solve each equation. Show all your work and CHECK!

12.
$$6x = -3x + 7$$

13.
$$4h = -2(3h + 5)$$

14.
$$18 = -3y$$

15.
$$\frac{x}{-5} = 8$$

16.
$$-5(3-x) = 3x + 1$$

Solve each inequality and graph the solution on a number line. Show all your work. Remember, if you multiply or divide by a negative number you must switch the direction of the inequality sign.

17.
$$x - (-4) > 9$$

18.
$$\frac{x}{-2} < 3$$

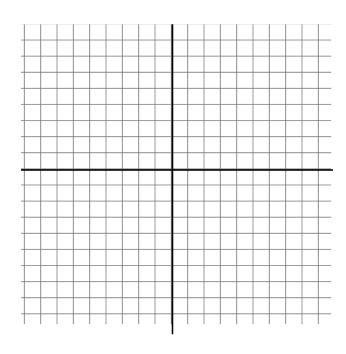


19.
$$3n + 5 \ge -4$$

Graph the equation. Use a table or the slope-intercept method, y = mx + b.

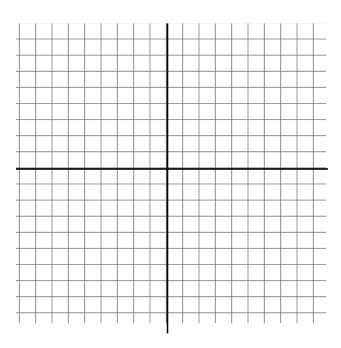
20.
$$y = -2x + 3$$

20.
$$y = -2x + 3$$
 slope: _____ y-intercept: _____



Graph the inequality. Don't forget to shade the solution area and to show your check.

21.
$$y < 2x - 3$$

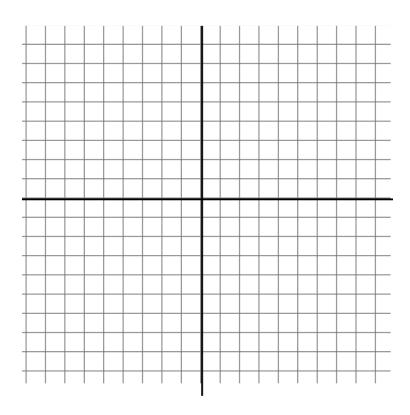


Find the slope of the line containing the points.

22. (-3, 11) and (2, 6)

Find the **x-intercept and y-intercept**. **Graph** the points. Find the **slope** of the line through the points. Write the equation in **slope-intercept** (y = mx + b) form.

23.
$$6x - 4y = 12$$



Simplify the following expressions.

Example:
$$3(m^2 + n) - 2(3m^2 - 4n) = 3m^2 + 3n - 6m^2 + 8n = -3m^2 + 11n$$

24.
$$(3x^2 + 4x - 5xy) + (-7x^2 + 6x - 5xy)$$

25.
$$(5y^3 - 3y + 4) + (2y^2 + 6y - 4y^3) - (9y^2 - 6 + 2y^3)$$

Use the distributive property to expand the product. Follow the example.

EXAMPLE:
$$(x + 4)(2x - 11) = 2x^2 - 11x + 8x - 44 = 2x^2 - 3x - 44$$

26.
$$(x-7)(x+5)$$
 27. $(y-8)(y+8)$

Factor each into the product of two binomials. Follow the example.

EXAMPLE:
$$x^2 + 6x - 7 = (x - 1)(x + 7)$$

28.
$$x^2 - 10x + 24$$

29.
$$x^2 - 81$$

30.
$$x^2 - 8x - 20$$

Factor each and solve for x. Follow the example.

EXAMPLE: $x^2 + 5x - 6 = 0$

(x+6)(x-1)=0

(x + 6) = 0 **OR** (x - 1) = 0

x = -6 OR x = 1

Factored and equal to 0
Either factor may equal 0

31.
$$x^2 + 6x + 8 = 0$$

32.
$$x^2 - 3x - 4 = 0$$

Solve by using the substitution or elimination method. The problems are on next page.

EXAMPLE Substitution:
$$y = 3x - 4$$
 and $8x - 2y = 10$

$$8x - 2(3x - 4) = 10$$
 Substitute the value for $y = 3x - 6x + 8 = 10$

$$2x + 8 = 10$$

$$2x = 2$$

$$x = 1$$
 Finish solving: $y = 3(1) - 4$ so $y = -1$.
Then CHECK! $8(1) - 2(-1) = 10$
 $8 + 2 = 10$ yes

EXAMPLE Elimination:
$$4x + 6y = 12$$

$$4x - 8y = 5$$

$$14y = 7$$
Subtract the two equations to get ----
$$y = \frac{1}{2}$$

Finish solving for x: 4x + 6(.5) = 12, so x = 9/4.

Then CHECK!
$$4(9/4) - 8(1/2) = 5$$

$$9-4 = 5 \text{ yes}$$

$$33. \qquad 2y + x = 5$$
$$y = 3x - 1$$

34.
$$x = 3 + y$$

 $x - 7y = 45$

RULES FOR SIMPLIFYING RADICALS (square roots)

$$a\sqrt{b} \times c\sqrt{d} = ac\sqrt{bd}$$

$$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{a/b}$$

$$a\sqrt{b} \times c\sqrt{d} = ac\sqrt{bd}$$
 $\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{a/b}$ $\sqrt{a} \times \sqrt{a} = \sqrt{a^2} = |a|$

$$a\sqrt{b} + c\sqrt{b} = (a+c)\sqrt{b}$$

Remember, proper form for radicals means:

- a. No perfect square factor under the radical. For example, $\sqrt{45} = \sqrt{9} \times \sqrt{5} = 3\sqrt{5}$.
- b. No fractions/decimals may be left under the radical. For example, $\sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{\sqrt{4}} = \frac{\sqrt{3}}{2}$.
- c. No radical may be left in the denominator of a fraction. For example,

$$\sqrt{\frac{3}{7}} = \frac{\sqrt{3}}{\sqrt{7}} = \frac{\sqrt{3}}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}} = \frac{\sqrt{21}}{7}. \text{ Another example, } \frac{15\sqrt{75}}{20\sqrt{21}} = \frac{3\sqrt{25}\sqrt{3}}{4\sqrt{7}\sqrt{3}} = \frac{3\times5}{4\sqrt{7}} = \frac{3\times5\times\sqrt{7}}{4\sqrt{7}\sqrt{7}} = \frac{15\sqrt{7}}{28}.$$

Simplify each. Leave in best radical form. NO DECIMAL EQUIVALENTS.

35.
$$\sqrt{32}$$

$$36. \qquad \frac{\sqrt{64}}{\sqrt{16}}$$

37.
$$\sqrt{20} - \sqrt{80}$$

$$38. \qquad 4\sqrt{5} \times 3\sqrt{10}$$